

UNIT - IV

8. (a) Find eigen values and eigen vector of

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

(b) Show that matrix $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$ is not diagonalizable over the field C .

9. Prove that every finite dimensional inner product space has an orthogonal basis.

Roll No.

3008

**B. Tech. 1st Semester (CSE)
Examination – February, 2022
MATH-1 (Calculus and LINEAR ALGEBRA)**

Paper : BSC-MATH-100-G

Time : Three Hours)

(Maximum Marks : 75

Begin answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard will be entertained after examination.

Note : Attempt five questions in all, selecting one question from each Unit. Question No. 1 is compulsory. All questions carry equal marks.

1. (a) Prove that $(\sin, \pi) = (k\pi, m)$.

(b) Compute $\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$.

(c) Find $|A|$ where the matrix $A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$

(d) Let $T: U \rightarrow V$ be a linear transformation the prove $T(0_U) = 0_V$ where 0_U and 0_V are zero vectors in U and V respectively.

(e) Let $T_1: R^2 \rightarrow R^2$ and $T_2: R^2 \rightarrow R^2$ be linear transforms, then verify that $T_1 T_2$ and $T_2 T_1$ are well defined or not.

(f) Define inner products space.

UNIT - I

2. (a) Examine for extreme values of

$$f(x, y) = 3x^2 - y^2 + x^3$$

(b) Show that

$$\log(x + h) - \log x = \frac{h}{x} - \frac{h^2}{2x^2} + \dots + (-1)^{n-1} \frac{h^{n-1}}{(n-1)x^n} + \dots$$

3. (a) Find the volume of solid formed by revolution about x-axis of loop of the curve $y = \left\{ \frac{ax^2 + x^2}{(a-x)} \right\}^{1/2}$

(b) Show that $\int_0^a \frac{y^{n-1}}{(1+y)^{n+1}} dy$

UNIT - II

4. (a) Solve following equations with the help of matrices:

$$x + y + z = 3, \quad x + 2y + 3z = 4, \quad x + 4y + 9z = 0$$

2008-2100-0-410-01201

(2)

(b) Show that vectors $v_1 = (1, 2, 4)$, $v_2 = (2, -1, 3)$, $v_3 = (0, 1, 2)$ and $v_4 = (-3, 7, 2)$ are C.O and find relation between them.

5. (a) Using Gauss-Jordan method find inverse of matrix

$$\begin{bmatrix} 8 & 4 & 3 \\ 2 & 1 & 1 \\ 1 & 2 & 1 \end{bmatrix}$$

(b) Solve the following equations by Cramer's rule
 $ax + y - 3z = 5, \quad x + 3y - 2z = 5, \quad 2x + y + 4z = 8$

UNIT - III

6. (a) If $P(x)$ denotes the set of all polynomials in x over a field F , then show that $P(x)$ is a vector space over F with vector addition as polynomial's addition and scalar multiplication defined as product of polynomial by an element of F .

(b) Examine the linear independence of the following vectors

$$(1, 1, 1), (1, 2, 3), (0, 1, 2) \text{ in } R^3$$

7. (a) Verify that mapping $T: R^3 \rightarrow R^3$ defined by $T(x, y, z) = (2x - 3y, 2y + 2z)$ is linear transformation.

(b) Find a linear transformation $T: R^3 \rightarrow R^3$ where range space is spanned by vectors $(1, 2, 3), (4, 5, 0)$

2008-2100-0-410-01201

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